

Semplificare le seguenti espressioni contenenti addizioni, moltiplicazioni e divisioni di frazioni algebriche.

232. $\left(\frac{1}{a} + \frac{1}{b}\right) : \left(\frac{1}{a^2} - \frac{1}{b^2}\right); \quad \frac{x^3 - y^3}{x^2y^2} : \left(\frac{1}{y^2} + \frac{1}{xy} + \frac{1}{x^2}\right) \cdot \frac{1}{x-y}. \quad \left[\frac{ab}{b-a}; 1\right]$

233. $\left(y^2 - \frac{1}{x^2}\right) : \frac{x^2y^2 + 1 - 2xy}{x^5}; \quad \left(1 - \frac{1}{b^2}\right) : \frac{b+1}{b}. \quad \left[\frac{x^3(xy+1)}{xy-1}; \frac{b-1}{b}\right]$

234. $\left(x^2 - \frac{1-x^2}{y^2-1}\right) : \frac{x^2y^2 + 2xy + 1}{y^2 + 2y + 1}; \quad \left[t^2 - \left(\frac{a}{b}\right)^2\right] : \frac{bt+a}{b^2}. \quad \left[\frac{(xy-1)(y+1)}{(y-1)(xy+1)}; bt-a\right]$

235. $\left(1 - \frac{x^3}{y^3}\right) : \left(1 - \frac{x}{y}\right) - \left(1 + \frac{x}{y}\right)^2; \quad \left(\frac{1}{a} + \frac{1}{b} - \frac{2}{a+b}\right)^3 : \left(\frac{a}{b} + \frac{b}{a}\right)^3. \quad \left[-\frac{x}{y}; \frac{1}{(a+b)^3}\right]$

236. $\frac{xy(y-x)}{x+y} : \left[\left(\frac{y}{x} - \frac{x}{y}\right) : \left(\frac{1}{y} + \frac{1}{x}\right)^2\right]; \quad \left(\frac{1}{x} + \frac{1}{y}\right) : \left(\frac{1}{x} - \frac{1}{y}\right) : \frac{2y+2x}{x^2 - 2xy + y^2}. \quad \left[1; \frac{y-x}{2}\right]$

237. $\left(\frac{x}{x-y} + \frac{y}{x+y}\right) : \left(\frac{x}{x-y} - \frac{y}{x+y}\right); \quad \left(2 - \frac{2m-n}{m-n}\right) : \left(\frac{m+n}{m-n} - 1\right). \quad \left[\frac{x^2 + 2xy - y^2}{x^2 + y^2}; -\frac{1}{2}\right]$

238. $\frac{r^2 - s^2}{r^2s + rs^2} : \left(\frac{r}{s} \cdot \frac{r^2 - s^2}{2r}\right); \quad \left(\frac{2x}{x-b} - \frac{2b}{x+b}\right) : \left(\frac{3x}{x-b} - \frac{3b}{x+b}\right). \quad \left[\frac{2}{r(r+s)}; \frac{2}{3}\right]$

239. $\left[\frac{x^4 - y^4}{x^2y^2} : \left(\frac{x}{y} + \frac{y}{x}\right)\right] \cdot \left(\frac{1}{x-y} - \frac{1}{x+y}\right). \quad \left[\frac{2}{x}\right]$

240. $\left(\frac{a^2 - a}{a-2} : \frac{a^2 - 3a}{a-2}\right) : \left(\frac{a}{a-3} - 1\right); \quad \left[\frac{x^4 - y^4}{(x-y)^2} : \frac{x^2 + xy}{x-y}\right] : \left(x + \frac{y^2}{x}\right). \quad \left[\frac{a-1}{3}; 1\right] \quad (6)$

241. $\left[\left(\frac{a^2 + b^2}{ab} + 2\right) : \left(\frac{a^2 + b^2}{ab} - 2\right)\right] : \frac{1}{(a-b)^2}. \quad [(a+b)^2]$

242. $\left[\left(\frac{x^2 + y^2}{x^2 - y^2} - 1\right) : \left(\frac{x^2 - y^2}{x^2 + y^2} + 1\right)\right] \cdot \left(\frac{1}{x^2} - \frac{1}{y^2}\right). \quad \left[-\frac{x^2 + y^2}{x^4}\right]$

243. $\left(\frac{5a}{5a+2b} + \frac{2b}{5a-2b}\right) : \left(\frac{5a}{5a-2b} - \frac{2b}{5a+2b}\right). \quad [1]$

244. $\left(\frac{2a+1}{a-3} : \frac{3a-1}{a+3} - \frac{2a}{a+1}\right) : \left(\frac{2a-1}{a+3} - \frac{2a-5}{a+1} - \frac{14}{a^2+4a+3}\right). \quad [Impossibile]$

245. $\left[\left(\frac{a-3b}{a-2b} - \frac{2a+4b}{2a+3b}\right) \cdot \frac{a-2b}{3a+b} + \frac{b}{2a-3b}\right] : \frac{b^2}{4a^2 - 9b^2}. \quad [6]$

246. $\left[\left(a + \frac{1}{a+b}\right) : \frac{a+b}{ab+a^2+1}\right] : \frac{a^4 + a^2b^2 + 1 + 2a^3b + 2a^2 + 2ab}{(a+b)^2}. \quad [1]$

247. $\left[\left(x - \frac{1}{x}\right) : \frac{x^4 - 1}{x^3y^2}\right] : \frac{xy}{x^2 + 1}. \quad [xy]$

248. $\left(p + \frac{q-p}{1+pq}\right) : \left(1 - \frac{1+pq}{pq-p^2}\right); \quad \left(\frac{m^3}{n^3} - \frac{n^3}{m^3}\right) : \left(\frac{m}{n} - \frac{n}{m}\right) \cdot \left[\frac{pq(p-q)}{1+pq}; \frac{m^4 + m^2n^2 + n^4}{m^2n^2}\right]$

249. $\left[\left(\frac{a+2}{a-1} - \frac{a-3}{a+1}\right) \cdot \frac{1}{14a-2} + \frac{1}{8a+8} \cdot \left(1 - \frac{1}{a}\right)\right] : \frac{a+1}{64a^2}. \quad \left[\frac{8a}{a-1}\right]$

Esercizi proposti

Eseguire le seguenti divisioni (o moltiplicazioni) tra frazioni algebriche.

- 215.** $\left(\frac{4x^2y}{5a^2b} : \frac{2xy^2}{15ab^2}\right) \cdot \left(\frac{y}{6x} : \frac{b}{a}\right); \quad \left(-\frac{5x^3y^2z}{4a^3b^3} : \frac{10x^4y^5z^3}{3a^4b^5}\right) \cdot \left(-\frac{8xy^3z^2}{ab^2}\right).$ [1; 3]
- 216.** $\frac{16a^5b^7}{(3+t)^5} : \frac{(2ab)^6}{(9-t^2)^4}; \quad \frac{(a+b)^2}{a-b} : \frac{a+b}{(a-b)^2}. \quad \left[\frac{b(3-t)^4}{4a(3+t)}; a^2 - b^2\right]$
- 217.** $\frac{5x-2}{x-3} : \frac{x+2}{4x-12}; \quad \frac{a^2-b^2}{ab} : \frac{(a+b)^2}{a^2}. \quad \left[\frac{4(5x-2)}{x+2}; \frac{a(a-b)}{b(a+b)}\right]$
- 218.** $\frac{x^3-y^3}{x^3+y^3} : \frac{2x-2y}{x^2-xy+y^2}; \quad \frac{a^4-b^4}{(a+b)^2} : \frac{a-b}{a^2+ab}. \quad \left[\frac{x^2+xy+y^2}{2x+2y}; a^3+ab^2\right]$
- 219.** $\frac{1}{a^4+ab^3} : \frac{1}{a^2+ab}; \quad \frac{(a-b)^2}{a^3-b^3} : \frac{a-b}{a^2+ab+b^2}. \quad \left[\frac{1}{a^2-ab+b^2}; 1\right]$
- 220.** $\frac{x-y}{3y} : \frac{x^2-y^2}{4xy}; \quad \frac{2a-8}{3a-15} : \frac{a^2-16}{a^2-25}. \quad \left[\frac{4x}{3(x+y)}; \frac{2(a+5)}{3(a+4)}\right]$
- 221.** $\frac{x^2+3x}{4xy-16y} : \frac{x+3}{3x-12}; \quad \frac{a^2-4a+4}{3a^2-27} : \frac{a^2-4}{a^2-6a+9}. \quad \left[\frac{3x}{4y}; \frac{(a-2)(a-3)}{3(a+2)(a+3)}\right]$
- 222.** $\frac{x^2+xy}{x^2+y^2} : \frac{x^3y+2x^2y^2+xy^3}{x^4-y^4}; \quad \frac{x^2-3x+2}{x^2-6x+9} : \frac{x^2-2x+1}{x^2-5x+6}. \quad \left[\frac{x-y}{y}; \frac{(x-2)^2}{(x-1)(x-3)}\right]$
- 223.** $\frac{a^3-b^3}{a^2b^2-a^4} : \frac{a^2+ab+b^2}{ab^2+b^3}; \quad \left(\frac{a^4+8a}{2a+4}\right)^3 : \left(\frac{a^4-2a^3+4a^2}{a^2+2a}\right)^3. \quad \left[\frac{-b^2}{a^2}; \frac{(a+2)^3}{8}\right]$
- 224.** $\frac{a^3-9a}{a^2-3a-10} : \frac{a^2+6a+9}{a-5}; \quad \frac{z^3-x^3}{6z^3x^3} : \left(\frac{z^2+zx+y^2}{4z^2x^2} \cdot \frac{z^2-x^2}{3z+3x}\right). \quad \left[\frac{a(a-3)}{(a-2)(a+3)}; \frac{2}{zx}\right]$
- 225.** $\frac{a^2+ab+b^2}{a^3+b^3} : \frac{a^3-b^3}{a^2-ab+b^2}; \quad \frac{y^2+(a+c)y+ac}{y^2+(b+c)y+bc} : \frac{y^2-a^2}{y^2-b^2}. \quad \left[\frac{1}{a^2-b^2}; \frac{y-b}{y-a}\right]$
- 226.** $\frac{(a+b) \cdot (a^2-ab+b^2) + 3ab(a+b)}{a^3+b^3} : \frac{(a+b)^2}{a^2-ab+b^2}$ [1]
- 227.** $\frac{a^2+b^2+2ab-c^2}{c^2-a^2-b^2+2ab} : \frac{a+b+c}{b+c-a}; \quad \frac{3a+3b}{4x-4} : \frac{bx+ax-b-a}{x^2-1} \quad \left[\frac{a+b-c}{a-b+c}; \frac{3(x+1)}{4(x-1)}\right]$
- 228.** $\left(\frac{a^4+a^2b^2+b^4}{x^2+y^2} : \frac{a^6-b^6}{x^4-y^4}\right) \cdot \left(\frac{a+b}{x+y} : \frac{x-y}{a-b}\right).$ [1]
- 229.** $\left(\frac{1-a^2-b^2-2ab}{4+4a+4b} : \frac{a+b-1}{2a^2+2ab}\right) : \frac{a^2-b^2}{2a^3}.$ $\left[\frac{a^4}{b-a}\right]$
- 230.** $2a^p : 4a^2; \quad 3a^{2p}b^{p+1} : (-2a^p b).$ $\left[\frac{1}{2}a^{p-2}; -\frac{3}{2}a^p b^p\right]$
- 231.** $-\frac{3}{7}x^{-5}y^{2q} : \left(-\frac{1}{14}x^{-p}y^{q+1}\right).$ $[6x^{p-5}y^{q-1}]$

- 250.** $\left[\left(a + \frac{a}{a+2} \right) : \left(a - \frac{a}{a-2} \right) - 1 \right] : \left(\frac{a+1}{a-3} - \frac{a+4}{a+2} \right).$ $\left[\frac{a}{a+7} \right]$
- 251.** $\left[\left(\frac{x+y}{x-y} + \frac{x-y}{x+y} \right) : \left(\frac{x^2+xy}{y} + \frac{xy+y^2}{x} \right) \right] : \left(\frac{1}{y} + \frac{1}{x} \right).$ $\left[\frac{2}{x^2-y^2} \right]$
- 252.** $\left(\frac{x+y}{x-y} - 1 \right) : \left(1 - \frac{x-y}{x+y} \right); \quad \left(\frac{a^2-a}{a-3} : \frac{a^3-a}{5a-15} \right) : \left(\frac{1}{a-1} - \frac{1}{a+1} \right).$ $\left[\frac{x+y}{x-y}; \frac{5(a-1)}{2} \right]$
- 253.** $\left(\frac{a^3-a^2}{a-5} : \frac{a^5-a^3}{2a-10} \right) : \left(\frac{1}{2a} - \frac{1}{2a+2} \right).$ [4]
- 254.** $\left[\left(\frac{a+b}{a-2} + 2 \right) : \left(\frac{a+b}{a-2} - 2 \right) \right] : \frac{1}{a-b-4}.$ [4 - 3a - b]
- 255.** $\left(\frac{b}{a^2-3ab+2b^2} + \frac{3b}{a^2+ab-6b^2} \right) : \left(\frac{3a}{a^2+2ab-3b^2} - \frac{a}{a^2-b^2} \right).$ $\left[\frac{2b \cdot (a+b)}{a(a-2b)} \right]$
- 256.** $\left(\frac{2x-3y}{x^2-y^2} - \frac{2}{x+y} + \frac{y^3}{x^4+xy^3-x^3y-y^4} + \frac{2xy}{x^3+y^3} \right) : \left(\frac{x+y}{x^2-xy+y^2} - \frac{1}{x+y} \right).$ $\left[\frac{1}{3} \right]$
- 257.** $\left(\frac{a+2}{a^2-9a+14} - \frac{5-a}{a^2-7a+10} + \frac{5-a}{a^2-12a+35} \right) : \left(\frac{7-9a}{a^2-6a-7} + \frac{a+2}{a-7} \right).$ $\left[\frac{a+1}{(a-2) \cdot (a-3)} \right]$
- 258.** $\left(\frac{a^2+4b^2}{a^3+2a^2b-ab^2-2b^3} + \frac{a+b}{a^2+ab-2b^2} - \frac{a-b}{a^2+3ab+2b^2} \right) : \frac{a^2+7ab+10b^2}{a^2-b^2}.$ $\left[\frac{1}{a+5b} \right]$
- 259.** $\left[\frac{ax}{b^2+x^3} \cdot \left(\frac{ab^3}{xy} - \frac{ax^5}{by} - \frac{b^3y}{ax} + \frac{x^5y}{ab} \right) \right] : \left(\frac{ab}{y} - \frac{ax^3}{by} + b - \frac{x^3}{b} \right).$ [a - y]
- 260.** $\left[\left(\frac{x^2}{y^2} + 1 + \frac{y^2}{x^2} \right) : \left(\frac{x}{y} + 1 + \frac{y}{x} \right) - 1 \right] : (x - y)^2.$ $\left[\frac{1}{xy} \right]$
- 261.** $\left[\left(\frac{1}{a-b} + \frac{1}{a+b} \right) : \frac{ab}{a^2-b^2} - 1 \right] : (2-b)^2.$ $\left[\frac{1}{b(2-b)} \right]$
- 262.** $\left[\left(\frac{x^2}{y^2} + \frac{1}{x} \right) : \left(\frac{x}{y^2} - \frac{1}{y} + \frac{1}{x} \right) - 1 \right] \cdot y.$ [x]
- 263.** $\left[\left(a + \frac{b-a}{1+ab} \right) : \left(1 - \frac{ab-a^2}{1+ab} \right) + a \right]^2 : (a^3+b^3).$ $\left[\frac{a+b}{a^2-ab+b^2} \right]$
- 264.** $\left[\left(\frac{1}{1+x} + \frac{x}{1-x} \right) : \left(\frac{1}{1-x} - \frac{x}{1+x} \right) - y \right] : (1-y^2).$ $\left[\frac{1}{1+y} \right]$
- 265.** $\left[\frac{22(a-b)^2}{21(a+b)} \cdot \frac{28}{33(b-a)} \cdot \left(-\frac{a+b}{8} \right) - \frac{a-b}{9} \right] : \frac{a^5+1}{a^4-1}.$ [0]
- 266.** $\left[\left(\frac{a}{a+b} + \frac{b}{a-b} \right) : \left(\frac{b}{a+b} - \frac{a}{a-b} \right) + b^2 \right] : (1-b) + b.$ [-1]
- 267.** $\left\{ \left[(1+x)^2 : \left(1 + \frac{1}{x} \right) - x \right] : \frac{x}{x+1} - x \right\} : \frac{x}{x+1}.$ [x(x+1)]
- 268.** $\left(\frac{a}{b} + \frac{b}{a} \right) : \left(\frac{a}{b} - \frac{b}{a} \right) + 1 : \left(1 + \frac{b}{a} \right) - 1 : \left(1 - \frac{b}{a} \right).$ $\left[\frac{a-b}{a+b} \right]$
- 269.** $\left(1 - \frac{x-3y}{x+y} \right) : \left(\frac{3x+y}{x-y} - 3 \right) - \left(\frac{y-2x}{x^2+y^2+2xy} - \frac{2}{x+y} \right) : \left(\frac{3}{y-x} - \frac{2y-x}{y^2-x^2} \right).$ [0]

Esercizi di riepilogo

Semplificare le seguenti espressioni.

286. $\left(\frac{x}{x+1} - \frac{x}{x-1} \right) \frac{1}{2x+2} - \frac{5}{x^2-1}$.

$$\left[\frac{6x+5}{(x+1)^2(1-x)} \right]$$

287. $\left(\frac{5}{a+b} - \frac{3}{a} \right) \left(\frac{7}{b} - \frac{1}{a-b} \right) + \frac{24}{ab} + \frac{37}{a^2-b^2}$.

$$\left[\frac{38a}{b(a^2-b^2)} \right]$$

288. $a \left(\frac{a-b}{a+b} - \frac{a+b}{a-b} \right) + b \left(\frac{a+b}{a-b} - \frac{a-b}{a+b} \right)$.

$$\left[-\frac{4ab}{a+b} \right]$$

289. $\left[a \left(\frac{a-b}{a+b} - \frac{a+b}{a-b} \right) \right] : \left[b \left(\frac{a+b}{a-b} - \frac{a-b}{a+b} \right) \right]$.

$$\left[-\frac{a}{b} \right]$$

290. $\left(\frac{x^3+x^2y+xy^2}{y^3-x^3} + \frac{x+y}{x-y} \right) \frac{x^2-y^2}{xy} + \frac{y+x}{y}$.

$$\left[\frac{(x+y)^2}{xy} \right]$$

291. $\left[\left(\frac{1}{x^3y} + \frac{y}{x^2} + \frac{1}{xy^2} \right) : \frac{y(1+2xy^2)-x(y^3-x)}{x^2y^2} \right] : \left(1 - \frac{1}{x} \right)$.

$$\left[\frac{1}{x-1} \right]$$

292. $\left(x-y + \frac{xy}{x+y} \right) \left(x+y - \frac{xy}{x-y} \right) \frac{xy+y^2}{(x^2+y^2)^2 - 5x^2y^2}$.

$$\left[\frac{y}{x-y} \right]$$

293. $\left[\left(1 + \frac{1}{a} \right) : \frac{1}{a} \right] \left[\left(a-1 + \frac{1}{a} \right) : \frac{1}{a} \right] : \left[\left(a^2 + \frac{1}{a} \right) (-a) \right]$.

$$[-1]$$

294. $\frac{x^2+ax+a^2}{x^2-a^2} \cdot \frac{\left(1-\frac{a}{x}\right)^2 \cdot \left(1+\frac{a}{x}\right)^2}{x^3-a^3}$.

$$\left[\frac{x+a}{x^4} \right]$$

295. $\left(\frac{1}{x} + \frac{1}{y} - \frac{z}{xy} \right) (x+y+z) : \left(\frac{1}{x^2} + \frac{1}{y^2} + \frac{2}{xy} - \frac{z^2}{x^2y^2} \right)$.

$$[xy]$$

296. $\left(\frac{5}{a-1} + \frac{5}{a-1} - \frac{10a^2}{1-a^2} \right) : \left(\frac{a}{a-1} + \frac{1-a}{a+1} - 1 \right)$.

$$\left[\frac{10(1+a)}{3-a} \right]$$

297. $\left[\left(1 + \frac{1}{a} + \frac{1}{a^2} \right) : \left(1 - \frac{1}{a^3} \right) \right] : \left(\frac{2}{a-1} - \frac{4}{a-2} \right) + \frac{(a-1)^2-1}{2a}$.

$$[0]$$

298. $\left(\frac{ab-ay+bx-xy}{a-x} + \frac{bx+by-xy-y^2}{x-a} \right) : \frac{ax-xy}{ab-ay-bx+xy}$.

$$\left[\frac{(b-y)^2}{x} \right]$$

299. $\left(\frac{x+1}{x-1} + \frac{x-1}{x+1} + \frac{4x}{1-x^2} \right) \left(1 + \frac{2x}{1-x} \right)$.

$$[-2]$$

300. $\left(\frac{3x+1}{x+y} \cdot \frac{x^2-y^2}{9x^2-1} + \frac{3x-1}{x-y} \frac{x^2-y^2}{9x^2-1} \right) : \frac{3x^2-y}{3x+1} + \frac{2}{3x+1}$.

$$\left[\frac{12x}{9x^2-1} \right]$$

301. $\left[\left(a+1 + \frac{1}{a-1} \right) : \left(a-1 + \frac{1}{a+1} \right) - \frac{a-1}{a+1} \right] : \left(\frac{1}{a+1} + \frac{1}{a-1} \right)$.

$$[2]$$

302. $\frac{5}{4} \left(\frac{5a^2+3a-2}{25a-10} + \frac{a^2}{2-5a} \right) \left(\frac{1}{3a-2} - \frac{1}{3a+2} \right) : \frac{1}{5a^2-2a}$.

$$\left[\frac{a}{3a+2} \right]$$